Computer Simulations of Brain Oxygenation at the Microvascular Level Validating a New Role of the Arterioles

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Abstract

Brain physiology critically depends on constant oxygen supply to the neurons to ensure various energy–dependent functions of the central nervous system. A volume of latest experimental data on oxygen metabolism obtained with high temporal and spatial resolution, with both invasive and non-invasive methods, and the use of technologies of various degrees of sophistication, strongly suggests arteriole involvement in brain oxygenation. This new approach challenges the traditional views on brain oxygenation according to which oxygen supply to the brain tissues occurs by diffusion at the capillary level.

In this research, a computer simulation of brain oxygenation at the microvascular level has been carried out to assess the role of the arterioles in the process. The model is based on the convective nanoﬂuidic (CNF) mechanism of brain water metabolism involved in oxygen mass-transfer [1,2]. The carried out simulations demonstrate that the arteriole oxygen supply dominates over the capillary oxygen delivery. The oxygen supply rates by arterioles can well meet the neuronal demands. The model accounts for some oxygen partial pressure (PO₂) distribution patterns in the brain that are hard to explain from the conventional capillary-oxygen-diffusion theory.

Keywords: Brain Oxygenation; Arterioles; Computational Model and Simulations; Convective Nanoﬂuidic Mechanism

Introduction

Brain physiology critically depends on constant oxygen supply to the neurons to ensure various energy–dependent functions of the central nervous system. In energy terms, the brain accounts for over 20% of total body oxygen metabolism with the neurons consuming 75%–80% of the energy produced by the brain mitochondrial system [3]. The brain lacks any substantial energy reserve and entirely depends on the cerebral microcirculation, which responds quickly and locally to the metabolic needs of neurons via neurovascular coupling during neuronal activation [4-6].

Information on PO₂ distribution in the brain and PO₂ mapping is crucial for understanding cerebral oxygen metabolism and building any realistic model of brains oxygenation. PO₂ of the brain has been studied across species in some detail using technologies of various degree sophistication, with high temporal and spatial resolution, both invasive and non-invasive ones [7-15].

The reported values for PO₂ in the cerebral arteries are 91-124 mm Hg [16-18]. PO₂ in larger pial arterioles with the diameter equal or over 40 µm is above 100 mmHg decaying to about 65 mmHg in the 10-µm arterioles [18,19]. PO₂ in the capillaries is 25–35 mm Hg [11,16,18,20] and in the cortical venues is 33-44 mmHg [16,18,21].

A research on the radial profiles of tissue PO₂ around arterioles yielded some rather unexpected findings. The periarteriolar PO₂ in the pial microvessels in normoxia was ~99 mmHg in the vessels of 230 µm diameter and ~ 73 mmHg in the vessels of ~22 µm diameter [22]. Overall, the tissue PO₂ values were in the range of ~ 5–100 mm Hg. with the higher values occurring in regions close to pial arterioles [8,9,18,20,23]. The brain tissue PO₂ around capillaries is about 15 – 29 mmHg [17,24,25].

Non-invasive measurement of cerebrospinal fluid PO₂ in humans using MRI visualisation makes it possible to obtain absolute PO₂ quantification [26]. It shows that PO₂ in the CSF of the cortical sulci is 106 ± 42 mm Hg [7,21,27,28]. On inhalation pure oxygen it rises up to 248 ± 50 Hg [27]. Considered against the PO₂ of 25–35 mm Hg in the capillaries, it poses a question if the capillaries may be the only oxygen supply source to the tissue. There is also an obvious disagreement between the high PO₂ in the venules and low oxygen in the capillaries.
Rapid oxygen enhancement and the high PO$_2$ values in sulcal CSF have been interpreted as an indication of a possible direct transfer of O$_2$ from the pial arterioles into the CSF [15,16,29]. Based on the accumulated data a conclusion has been drawn that all microvessels, but not exclusively the capillaries, may supply oxygen to brain tissue [16,18,30,31]. Contribution of the arterioles in supplying brain tissues with oxygen is stressed. The new evidence challenges the common views of capillaries as the major site of O$_2$ delivery [18].

Oxygen supply by capillaries to the surrounding tissue is based on the Krogh's oxygen diffusion mechanism [32]. The controversy about the oxygen supply mechanism asks for a paradigm shift and the use of other approaches to look into the problem [1,33,34].

Brain microvessels are highly permeable to water. The most active water-conducting aquaporin AQP4, involved in regulation of water flux through the blood-brain barrier (BBB), is expressed in the astrocyte endfeet enveloping the microvessels. It ensures kinetic control over water movement between the blood and the brain interstitial space [35-40]. The walls of the cortical arterioles are permeable to oxygen [16,31].

The brain extracellular space (ECS), an intricate network of nanoslits and nanochannels, is a conduit for the extracellular fluid (ECF). The ECS presents a nanofluidic domain where fluid movement is governed by the slip-flow mechanism [41,42]. The ECF, a mobile medium, surrounds all neurons and other components of the brain parenchyma and may serve a vehicle for oxygen, energy substrates, information molecules etc. There is constant convective exchange between the CSF and the ECF [43]. It should be noted that according to the orthodox views, the ECS presents a diffusion barrier to mass transfer [44-46].

The aims of the present research has been to build a computer model of oxygen metabolism at the microvascular level, based on the CNF mechanism, and to explore its oxygen-mass-transfer capacity with a special attention given to the function of the arteriolar section.

**Methods**

We consider a simplified linear microvascular array consisting of a feeding arteriole, a capillary and a draining venule [47]. This structure is modelled as two right frustums joined at the top (Figure 1). Contrary to the oxygen diffusion models [48,49], no restrictions are imposed on the spatial arrangement of these microvessels in respect to the neurons. The geometric characteristics of the microvessels and other pertinent parameters for the model have been obtained from the literature [50,51].

For clarity of presentation, the diameters of the microvessels are rendered about thirty times larger compared to the overall length of the system.

The simulations have been carried out in two steps: (i) evaluation of the radial water volumetric flow rates and (ii) evaluation of the molar oxygen mass-transfer rates in consideration of the water volumetric flow rates, oxygen solubility and oxygen molar volume.

To model the radial water fluxes we used Kedem-Katchalsky formalism, based on linear non-equilibrium thermodynamics [52]:

\[
J_v = L_p S \left( P_a - \Delta P x - f(t) - \pi_p + \pi_{ISF} \right),
\]

where $f_p$ is the volumetric flow rate of water (cm$^3$/s/mmHg per cm$^2$ transfer area); $L_p$ is an AQP4-dependent hydraulic conductivity coefficient (13.7 $10^4$ cm/s/mmHg) [1]; $S = LSA$ is the frustum lateral surface area (cm$^2$):

\[
LSA = \pi(R + r)\sqrt{(R - r)^2 + L^2},
\]
The spatiotemporal presentation of our simulation results reveals some interesting features about water metabolism in the microvascular system (Figures 2 and 3). The interplay of the hydrostatic and the oncotic pressure gradients outside of and inside the microvessels results in establishing distinct water flux patterns along the length of the microvascular array. Such patterns have been demonstrated in our earlier research on the brain water metabolism and the capillary water exchange [1]. Our present simulation, encompassing microvessels beyond exclusively capillary area, demonstrate different quantitative results.

\[ \Delta P = \frac{(P_a - P_d)}{L_{ad}}, \]  

(3)

Where \( P_a \) (mmHg) and \( P_d \) (mmHg) is the hydrostatic pressure at \( a \) and \( d \), respectively; \( P_v \) is the venular hydrostatic pressure (6.6 mmHg); \( L_{ad} \) is the overall length of the linear microvessel array (cm). \( x \) is a distance from \( a \) (cm) at any point on the longitudinal axis of the microvessel array.

\( f(t) \) is an analytical form for the intracranial pressure (ICP) as a function of time (for the ICP pressure waveforms shown in Figure 2). \( \pi_p \) is the plasma oncotic pressure (22 mmHg). \( \pi_{ISF} \) is the interstitial fluid oncotic pressure (1 mmHg).

The overall fluid transfer between the blood and the interstitial fluid is isosmotic [36,53] driven by the hydrostatic pressure gradients between the blood and the surrounding tissue [54-56]. The volumes of water transferred in various sections of the model have been found by numerical integration of Eqn. 1.

The molar oxygen mass transfer rates, \( dO_2 / dt \) (fmol/min per LSA), have been obtained from:

\[ dO_2 / dt = \alpha V_{H2O} S / V_m^{O2}, \]  

(4)

where \( \alpha \) is the Henry's law solubility constant \((2.80 \times 10^{-3} \text{ cm}^3 \text{O}_2/\text{cm}^3 \text{ at } 37 \degree \text{C and } 100 \text{ mmHg PO}_2)\); \( V_{H2O} \) is the volumetric flow rate of water \((\text{cm}^3/\min)\); \( V_m^{O2} \) is the molar volume of oxygen \( (193313 \text{ cm/mol at } 37 \degree \text{C and } 100 \text{ mmHg PO}_2)\).

The intracranial hydrostatic pressure (ICP) waveforms (Figure 2) have been digitized and approximated by analytical expressions using TableCurve. Computer simulations have been carried out using Mathematica 10 program and solved numerically [1,2].

Results

The spatiotemporal presentation of our simulation results reveals some interesting features about water metabolism in the microvascular system (Figures 2 and 3). The interplay of the hydrostatic and the oncotic pressure gradients outside of and inside the microvessels results in establishing distinct water flux patterns along the length of the microvascular array. Such patterns have been demonstrated in our earlier research on the brain water metabolism and the capillary water exchange [1]. Our present simulation, encompassing microvessels beyond exclusively capillary area, demonstrate different quantitative results.

Figure 2 shows water movement in the filtration and the reabsorption segments of the microvessels.

**Figure 2:** Water movement in the filtration and the reabsorption sections of the microvascular array
To simulate the effects of the changes in the volumetric blood flow on the radial water flux, the entrance diameter of the feeding arteriole was set to 40 µm, 60 µm and 80 µm. Table 1 demonstrates corresponding increases in the radial water flux and oxygen supply rates with the diameters.

An increase in the ICP (wave w2) results in a decrease of the radial water flux and the oxygenation rate.

With the axial dimension 0.0605 cm and the venule outlet diameter 60 µm, the RS reabsorbs about 14% of the filtrated water. The rest of the filtrated water gets into the ECF and, moving along the nanodimensional ECS, should be reabsorbed into either other venules or mix, eventually, with the bulk CSF.

On normobaric inhalation of 95% oxygen there is observed a considerable increase of oxygen partial pressure in the microvessels and surrounding tissues reaching 241 mHg O2 in arterioles 30 μm diameter [31]. This is translated into a 2.41- times increase in the oxygen supply rate by the CNF mechanism.

In Figure 3 there are presented results on water exchange within the oscillatory section of the microvascular system.

Compared to the FS, the radial water fluxes within the OS are low. As has been suggested before, the oscillatory pattern of water fluxes in the OS, as shown by the bar graph, facilitates fast informational exchange between the brain and the systemic blood [1]. The frequency of this exchange is controlled by the heart beat rate.

<table>
<thead>
<tr>
<th>No</th>
<th>Feeding arteriole diameter at a, cm x 10^-4</th>
<th>Hydrostatic pressure at a, mmHg</th>
<th>ICP wave max/ min, mmHg</th>
<th>LSA, cm^2</th>
<th>Radial water flux, cm^3/min x 10^-4</th>
<th>Oxygen supply rate in normoxia†, fmol/min</th>
<th>Oxygen supply rate in hyperoxia ††, fmol/min</th>
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</thead>
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<tr>
<td>1</td>
<td>40</td>
<td>66</td>
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<td>26.9</td>
<td>64.8</td>
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<td>66</td>
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<td>66</td>
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<td>16.3</td>
<td>3.26</td>
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<td>114.0</td>
</tr>
<tr>
<td>4</td>
<td>80</td>
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<td>15.0/ 2.0</td>
<td>15.0</td>
<td>2.40</td>
<td>34.8</td>
<td>83.9</td>
</tr>
</tbody>
</table>

\*Wave w1; **Wave w2; †Respiration with 21% oxygen; ††Respiration with 95% oxygen

Table 1: Parameters of water movement and oxygen supply rate within the FS in the microvascular array

OS+ presents the filtrated water and OS- the reabsorbed water. Pl indicates the infinite plane passing through the minimum at 0.14 s. The bar graph in the right top corner presents the volumes of the filtrated (1) and the reabsorbed (2) water over a complete cardiac cycle.

Figure 3: Simulation results on water movement in the oscillatory section of the microvascular system
Discussion

A large body of evidence and experimental results on oxygen partial pressure distribution in the brain challenges the capillary oxygen diffusion theory of brain oxygenation. It asserts that the arterioles may play a key role in oxygen supply to the cerebral tissue [16,18,30,31,57]. This controversy directly touches upon the mechanisms of brain oxygenation.

In our simulations, we employed a simple linear microvascular array of an arteriole, a capillary and a venule to investigate the extent of involvement of a particular arteriolar section in the oxygen exchange. The model is based on the CNF mechanism of brain water metabolism engaged in oxygen mass transfer in the brain tissues [1,2].

Our results demonstrate that the arteriole section of the array presents the main source of oxygen supply. The obtained oxygen supply rates of 26.9 - 47.3 fmol/min, in normoxia, and 64.8 - 114.0 fmol/min, in hyperoxia, are well compared with the oxygen consumption rate by an average neuron of the human brain, 27.4 fmol/cell/min [58], and by an average neuron of the brain across species, 0.66 - 60.0 fmol/cell/min [58,59].

In this research, we concentrated only on small-diameter arterioles. There is evidence that larger arterioles may equally supply oxygen to the surrounding tissues [16,18,30,31,60]. Considering all that, one may well assume that within the arteriolar networks there would be even higher oxygen supply rates compared to those obtained on a simple microvascular system under study in this paper.

Our earlier simulations carried out on a capillary model give oxygen supply rate of 0.88 fmol/min [2]. The arteriolar rates are thus 30 - 53 times higher than the capillary ones. This underscores the metabolic importance of arterioles in brain oxygenation.

Oxygen supply rate increases with an increase of the arteriole diameter (Table 1). Considered from the point of views of the regulation mechanism of neuronal oxygen-supply, it demonstrates the way the changes in the arteriole diameter influence the oxygen supply rates. This effect is observed in the neurovascular coupling, as a response to the neuronal activation [4-6,61,62].

Increasing intracranial hydrostatic pressure negatively reflects on brain oxygenation (Table 1, wave 2). It might serve as an early indication to the effect of a moderate increase of the ICP on brain energy metabolism.

A commonly accepted brain oxygenation mechanism is based on the oxygen diffusion theory put forward by Krogh where the flow of oxygen in the tissue is driven by a concentration gradient of oxygen between the blood to the cells [48,63]. Diffusion mechanism intrinsically sets limits for the critical radius of 30 to 40 μm around a capillary within which sufficient oxygenation of the tissue is only possible [64]. There are other limitations of diffusion when applied to the brain [59]. The spatial organization of the vascular system where oxygen content is higher than in tissue, is a key factor for maintaining effective oxygen supply [65]. Contrary to diffusion, the CNF mechanism of brain oxygenation is free of distance limitations or restrictions on spatial organization [1,2].

There are some observations that are difficult to explain by the oxygen diffusion mechanism alone operating at the capillary level [66-68]. For example, PO2 in the outflowing blood of the cortical venules is higher than in the capillaries [16]. It is by 39% higher in the CSF than in the venous blood [14]. PO2 in the sulcal CSF is close or equal to that in the arterial blood and from 4 to 5 times higher than in the capillary blood [27].

To cope with this situation we have put forward a conceptual view of a convective extracapillary transfer of oxygen [68,69] and further explored this issue within a nanofluidic approach to brain water metabolism [1,2,70].

Extremely energy demanding neural activity is coupled to the mitochondrial energy production and critically depends on tissue oxygenation [71,72]. The local oxygen consumption rates, depending on the neuronal activity, may change by a factor of about five [64]. Monitoring the redox-state of the components of the mitochondrial electron transfer chain makes it possible to closely study respiratory functions of the mitochondria, both in vitro and in vivo [73]. The intensity of mitochondrial respiration is commonly assessed on the basis of the NAD+/NADH ratio [74].

In our earlier research, we studied, in an open-system device, the NAD+/NADH ratio in mitochondria under the controlled oxygen supply rates. The zero-order kinetics of the oxygen consumption rates by the mitochondria continued down to the critical PO2 = 1 mm Hg. Below that value, the mitochondria entered the controlled hypoxic states characterized by uncoupling of oxidative phosphorylation the extent of which depended on the level of the hypoxia. The hypoxic uncoupling was fully reversed on return to normoxia [75-77].

NADH fluorescence imaging has been used to study in vivo the effect of AQP4 deletion on oxygen microdistribution. Deletion of Aqp4 increases NADH fluorescence, a sign of tissue hypoxia, in the areas furthest away from cerebral microvessels. This, for the first time, clearly demonstrates AQP4 participation in the oxygen supply [78]. The fact that AQP4 deletion manifests itself furthest away from the cerebral microvessels excludes the diffusion mechanism of oxygen transport with its critical oxygenation radius. At the same time, it fully agrees with functioning of the CNF mechanism of brain oxygenation.

The CNF mechanism explains the enhancement of the venular PO2. Indeed, in the microvascular arrangement under study, the venular RS reabsorbs 14% of the water filtrated in the FS. This flux carries oxygen to the venule thus increasing the PO2 in the outflowing blood.
The steady-state level of PO$_2$ in the sulcal CSF of about 106 mmHg is notably high and at least 3-4 times over that of the capillary PO$_2$ [21,27]. The subpial zone is characterized by the absence of capillary vessels [79]. High oxygen consumption by the surrounding tissue asks for equally high oxygen supply rate to maintain a steady-state level of PO$_2$. In this situation, the capillaries are unlikely oxygen suppliers by the diffusion mechanism. It is the pial arteriolar network, with the walls of arterioles permeable to oxygen, that presents a most probable source of oxygen for the sulcal CSF [16,22,80]. The close values of PO$_2$ in both the arterioles and the CSF would further preclude a fast oxygen supply rate by diffusion. Oxygen supply there may be realized through the CNF mechanism instead.

The computational model of brain oxygenation, based on the CNF mechanism, demonstrates a good oxygen-supply capability for the arterioles. Within the framework of this model there are found explanations for the experimental observations on the arteriolar involvement in oxygen supply including those results that are difficult or impossible to explain within the conventional capillary diffusion theory.

Conclusion

Brain function critically depends on continuous oxygen supply by the bloodstream. A commonly accepted view on brain oxygenation centers on the capillaries as the main source of oxygen for the brain tissues. The progress in the technology of oxygen assessment and mapping in the brain, along with the new accumulated experimental data, challenge the exclusive role of the capillaries in brain oxygenation and suggests the arterioles as an alternative source of oxygen.

Carried out computer simulations of brain oxygenation demonstrate that the arterioles present an important source of oxygen for the neurons dominating over the capillary supply. Contrary to the diffusion-based orthodox theory, oxygen mass transfer is realized through the CNF mechanism of brain water metabolism [1,33]. The simulations account for the ‘anomalous’ oxygen partial pressure distribution in the brain tissues and the increase of oxygen in the outflowing venous blood, the observations that are difficult to explain from the conventional capillary-oxygen-diffusion theory. The simulations underscore the important role of the arterioles in brain oxygenation.

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Conflict of Interest Declaration

The author declares no competing financial interests.

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